# 1 <br> <br> Money Math for Teens 

 <br> <br> Money Math for Teens} Introduction to Earning Interest: 9th and 10th Grades Version


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## Introduction to Earning Interest: APR, APY and Compound Interest <br> 9th and 10th Grades Lesson Plan

## OBJECTIVE

Saving and investing money safely and wisely are critical skills for people of all ages and backgrounds. Armed with the knowledge of how investments work, savvy investors can make informed decisions and determine the best investment choices available to them.

Students will:

- Learn and use investment vocabulary
- Discover the concept of compound interest and understand its effect on savings
- Compute simple and compound interest over a variety of compounding periods.


## TEACHING MATERIALS

- Lesson plan
- Teacher worksheet with precalculated examples
- Now You Try student worksheet with solutions
- Student assessment worksheet with solutions


## LESSON ACTIVITY

1. Discuss vocabulary words principal, deposit, interest, term, APR and APY.
2. Certificate of deposit (CD):

- Compounds annually.
- Work through precalculated examples of annual compounding (see teacher worksheet, Examples 1 and 2).
- Now You Try student worksheet: practice annual interest calculations (page 11).

3. Statement savings account:

- Compounds quarterly.
- Work through precalculated example of quarterly compounding (see teacher worksheet, Example 3).
- Note: The calculations presented do not take into account that different months have different numbers of days. Quarterly calculations are done by computing annual interest, then dividing by 4.
- Emphasize that annual interest paid quarterly > annual interest paid annually.
- Define and demonstrate how to calculate APY.
- Now You Try student worksheet: practice quarterly interest calculations (page 12).

4. Compound interest formula:

- Introduce the compound interest formula:

> Where: $\boldsymbol{A}=$ Accumulated balance $\boldsymbol{P}=\boldsymbol{P}=$ Principal $\boldsymbol{r}\left(\mathbf{1}+\frac{\boldsymbol{r}}{\boldsymbol{n}}\right)^{n t}$$\quad \begin{aligned} & \boldsymbol{n}=\text { APR expressed as a decimal } \\ & \boldsymbol{n}=\text { Number of compounding periods per year } \\ & \boldsymbol{t}\end{aligned}$

- Review the scenario outlined in Example 3, using the compound interest formula to calculate Michael's principal, interest and APY at the end of one year of quarterly compounding.
- The formula produces the same accumulated value $\mathbf{( \$ 8 , 1 6 1 . 2 0})$.
- The interest is still $\mathbf{\$ 1 6 1 . 2 0}$.
- The APY is still 2.015\%.
- Now You Try student worksheet: practice quarterly interest calculations using the compound interest formula (page 13).

5. Money market savings account:

- Compounds monthly.
- Work through precalculated example of monthly compounding (see teacher worksheet, Example 4).
- Note: The calculations presented do not take into account that different months have different numbers of days. Monthly calculations are done by computing annual interest, then dividing by 12.
- Calculate APY for the example.
- Now You Try student worksheet: practice monthly interest calculations (page 14).

6. Discussion: compare and contrast annual, quarterly and monthly compounding.
7. Evaluate students' comprehension (see assessment worksheet).

## Teacher Worksheet

## Vocabulary

Principal: An amount of money owned by an investor and held by a financial institution such as a bank.
Deposit(s): The act of establishing, or adding to, existing principal in an account (verb); the money placed in the account (noun).

Interest: The amount of money you earn by leaving deposits in a bank or financial institution. Interest is a percentage of your principal.
Term: The period of time an investment lasts.
Annual percentage rate (APR): The percentage rate at which interest is calculated annually.
Certificate of deposit (CD): An agreement between an investor and a bank (or financial institution) whereby the investor agrees to put a certain amount of money on deposit (this is the principal) for a certain amount of time without withdrawing it (this is the term) and the bank agrees to pay the investor interest at an agreed-upon percentage rate, known as the annual percentage rate (APR).

Compounding period: The amount of time that elapses between interest payments.

- Annual compounding: once per year
- Quarterly compounding: once every three months
- January - March: 1st quarter
- April - June: 2nd quarter
- July - September: 3rd quarter
- October - December: 4th quarter
- Monthly compounding: once per month

Compound interest: Interest calculated on both the principal you have on deposit and on interest that has accumulated in the past.

# Introduction to Earning Interest: APR, APY and Compound Interest 

## Principal and Interest

## Example 1

Michael is saving money to buy a car. He takes $\$ \mathbf{8 , 0 0 0}$ to the bank and opens an annual CD upon which the bank agrees to pay him $\mathbf{2 \%}$ interest.

| Principal | $=8000$ |
| :--- | :--- |
| Term | $=1$ year |
| APR | $=2 \%=0.02$ |
| $8000 \times 0.02$ | $=\$ 160$ |
| $8000+160$ | $=\$ \mathbf{8 , 1 6 0}$ |


| Beginning Balance | $2 \%$ Interest | Ending Balance |
| :--- | :--- | :--- |
| $\$ 8,000$ | $\$ 160$ | $\$ 8,160$ |

After one year, Michael has earned $\$ \mathbf{1 6 0}$ in interest on his initial deposit of $\$ 8,000$, so his balance is now \$8,160.

## Annual Compounding: Certificate of Deposit

## Example 2

Now, let's say Michael leaves his money in the bank for four years. The term of the annual CD is four years, so he will be earning $\mathbf{2 \%}$ interest per year for four years. Since this is an annual CD, interest will be added to the principal at the end of every year. This is called annual compounding.

|  | Beginning Balance | $2 \%$ Interest | Ending Balance |
| :--- | :--- | :--- | :--- |
| Year 1 | $\$ 8,000.00$ | $\$ 160.00$ | $\$ 8,160.00$ |
| Year 2 | $\$ 8,160.00$ | $\$ 163.20$ | $\$ 8,323.20$ |
| Year 3 | $\$ 8,323.20$ | $\$ 166.46$ | $\$ 8,489.66$ |
| Year 4 | $\$ 8,489.66$ | $\$ 169.79$ | $\$ 8,659.45$ |

## Now You Try

Ask students to do page 11 of the Now You Try student worksheet.

# Introduction to Earning Interest: APR, APY and Compound Interest 

## Quarterly Compounding: Statement Savings Account

## Example 3

Michael's bank offers other types of investment accounts in addition to certificates of deposit. One such type of account is a statement savings account. This type of account is similar to a certificate of deposit in that it also pays an annual percentage rate (APR) of interest, but there are some differences, too.
A statement savings account doesn't require Michael to promise not to take the money out for a specific period of time. Michael can go in and withdraw his money any time he wants. Also, instead of paying Michael his interest only once per year (annually), the bank will make an interest payment deposit into his account at the end of every quarter, because statement savings accounts compound quarterly.
When the bank makes an interest payment, the interest Michael earned during that quarter is added to his principal, and the new balance becomes Michael's new principal balance for the next quarter. Now Michael will begin earning interest on his interest! This is called compound interest.
Let's say Michael takes his $\$ 8,000$ to the bank and opens a statement savings account instead of a certificate of deposit. The bank is going to pay him the same $2 \%$ interest on this account that it was offering for the CD.

Michael's beginning principal amount is again $\mathbf{\$ 8 , 0 0 0}$. Also, his APR is still $\mathbf{2 \%}$. However, Michael gets interest compounded quarterly on this account.
At the end of the 4th quarter, what will Michael's principal balance be?

1. First, calculate his annual interest: $8000 \times 0.02=\$ 160$
2. Next, calculate what his 1st quarter interest payment will be: $160 / 4=\$ 40$
3. At the end of the 1st quarter, Michael's new principal balance will be $\mathbf{\$ 8 , 0 4 0}$.
4. Next, calculate the annual interest he will earn on $\$ 8,040$ : $8040 \times 0.02=\$ 160.80$
5. Calculate his 2 nd quarter interest payment: $160.80 / 4=\$ 40.20$
6. At the end of the $\mathbf{2 n d}$ quarter, Michael's new principal balance will be $8040+40.20=\mathbf{\$ 8 , 0 8 0 . 2 0}$.
7. Next, calculate the annual interest he will earn on $\$ 8,080.20: 8080.20 \times 0.02=\$ 161.60$
8. Calculate his 3rd quarter interest payment: 161.60/4 = \$40.40
9. At the end of the 3rd quarter, Michael's new principal balance will be $8080.20+40.40=$ $\$ 8,120.60$.
10. Finally, calculate the annual interest he will earn on $\$ 8,120.60: 8120.60 \times 0.02=\$ 162.41$
11. Calculate his 4th quarter interest payment: $162.41 / 4=\$ 40.60$
12. At the end of the 4th quarter, Michael's new principal balance will be $8120.60+40.60=$ $\$ 8,161.20$.

After four quarters have passed, Michael has had his money in the statement savings account for one year. His ending balance at the end of that year is $\mathbf{\$ 8 , 1 6 1 . 2 0}$.
Do you remember what his ending balance would have been if he had opened an annual CD instead? $(\$ 8,160)$

Let's compare these two choices.

- Which type of account would have earned Michael more interest? (Statement savings account)
- How much more interest would Michael earn by opening the statement savings account instead of the annual CD? (\$1.20)

Why? After all, both accounts pay the same 2\% APR.
If $2 \%$ of $\$ 8,000$ is $\$ 160$, and he earned $\$ 161.20$ on his principal in the statement savings account, then he must have actually earned more than $2 \%$ in the statement savings account.
This is because he earned interest on his interest during the year. His statement savings account yielded more than $2 \%$ for the year. This extra earning because of compounding interest is called annual percentage yield, or APY. APY is the actual rate your money earns, taking compounding into consideration.
To calculate the APY, we divide the amount of interest Michael earned for the year by his original principal deposit:
$A P Y=\frac{161.2}{8000}=0.02015=\mathbf{2 . 0 1 5} \%$

So a statement savings account that pays an APR of $\mathbf{2 \%}$ will earn an APY of $\mathbf{2 . 0 1 5 \%}$ because of the effect of compound interest.

## Now You Try

Ask students to do page 12 of the Now You Try student worksheet.

## Compound Interest Formula

As you can see, compounding several times per year and holding an investment for multiple years would make for a lot of manual calculations. Luckily, there is a formula called the compound interest formula that allows us to calculate the accumulated balance of an investment across multiple years and multiple compounding periods.
Introduce the compound interest formula:

$$
A=P\left(\mathbf{1}+\frac{r}{n}\right)^{n t} \quad \begin{array}{ll}
\boldsymbol{r}=\text { APR expressed as a decimal } \\
\boldsymbol{n}=\text { Number of compounding periods per year } \\
\boldsymbol{t}=\text { Number of years the investment lasts }
\end{array}
$$

Review the scenario outlined in Example 3:
Let's say Michael takes his $\$ 8,000$ to the bank and opens a statement savings account instead of a certificate of deposit. The bank is going to pay him the same $2 \%$ interest on this account that it was offering for the CD.
Michael's beginning principal amount is again $\mathbf{\$ 8 , 0 0 0}$. Also, his APR is still $\mathbf{2 \%}$. However, Michael gets interest compounded quarterly on this account.

Principal $(P)=8000$

$$
\begin{aligned}
& A=P\left(1+\frac{r}{n}\right)^{n t} \\
& A=8000\left(1+\frac{0.02}{4}\right)^{4 \times 1} \\
& A=8000(1+0.005)^{4} \\
& A=8000(1.005)^{4} \\
& A=8000(1.02015) \\
& A=\$ 8.161 .20
\end{aligned}
$$

Compare the interest calculated using the formula with the interest calculated when we did the calculation the long way, by hand. Notice that the amount of interest (\$161.20) matches.

## Now You Try

Ask students to do page 13 of the Now You Try student worksheet.

# Introduction to Earning Interest: APR, APY and Compound Interest 

## Monthly Compounding: Money Market Savings Account

## Example 4

Michael's bank offers another type of investment account similar to the statement savings account. This account is called a money market savings account. This type of account works just like a statement savings account except that the compounding period is monthly instead of quarterly. This means that Michael will receive an interest payment deposit into his account at the end of every month.
When that happens, the interest Michael earned in the previous month is added to his principal, and the new balance becomes Michael's new principal balance for the next month. So now Michael will begin earning interest on his interest monthly!

This time, Michael takes his $\$ 8,000$ to the bank and opens a money market savings account instead of a statement savings account. The bank is going to pay him the same $2 \%$ on this account that it was offering for the statement savings account.
Michael's beginning principal amount is again $\mathbf{\$ 8 , 0 0 0}$. Also, his APR is still $2 \%$. However, Michael gets interest compounded monthly on this account.
After three months, or one quarter, what will Michael's principal balance be?

1. First, calculate his annual interest: $8000 \times 0.02=\$ 160$
2. Next, calculate what his 1st month's interest payment will be: $160 / 12=\$ 13.33$
3. At the end of the 1st month, Michael's new principal balance will be $\mathbf{\$ 8 , 0 1 3 . 3 3}$.
4. Next, calculate the annual interest he will earn on $\$ 8,013.33$ : $8013.33 \times 0.02=\$ 160.27$
5. Calculate his 2 nd month's interest payment: $160.27 / 12=\$ 13.36$
6. At the end of the 2nd month, Michael's new principal balance will be $8013.33+13.36=$ $\$ 8,026.69$.
7. For the 3 rd month, calculate the annual interest he will earn on $\$ 8,026.69$ : $8026.69 \times 0.02=$ $\$ 160.53$
8. Calculate his 3rd month's interest payment: 160.53/12=\$13.38
9. At the end of the 3 rd month, Michael's new principal balance will be $8026.69+13.38=$ \$8,040.07.
At the end of three months, we have completed the 1st quarter.
What would Michael's balance have been at the end of the 1st quarter if he had a statement savings account compounding quarterly? $(\mathbf{\$ 8}, \mathbf{0 4 0})$

If we continue for all 12 months of the year:

|  | Beginning Balance | $2 \%$ Interest | Ending Balance |
| :--- | :--- | :--- | :--- |
| 1st month | $\$ 8,000.00$ | $\$ 13.33$ | $\$ 8,013.33$ |
| 2nd month | $\$ 8,013.33$ | $\$ 13.36$ | $\$ 8,026.69$ |
| 3rd month | $\$ 8,026.69$ | $\$ 13.38$ | $\$ 8,040.07$ |
| 4th month | $\$ 8,040.07$ | $\$ 13.40$ | $\$ 8,053.47$ |
| 5th month | $\$ 8,053.47$ | $\$ 13.42$ | $\$ 8,066.89$ |
| 6th month | $\$ 8,066.89$ | $\$ 13.44$ | $\$ 8,080.33$ |
| 7th month | $\$ 8,080.33$ | $\$ 13.47$ | $\$ 8,093.80$ |
| 8th month | $\$ 8,093.80$ | $\$ 13.49$ | $\$ 8,107.29$ |
| 9th month | $\$ 8,107.29$ | $\$ 13.51$ | $\$ 8,120.80$ |
| 10th month | $\$ 8,120.80$ | $\$ 13.53$ | $\$ 8,134.33$ |
| 11th month | $\$ 8,134.33$ | $\$ 13.56$ | $\$ 8,147.89$ |
| 12th month | $\$ 8,147.89$ | $\$ 13.58$ | $\$ 8,161.47$ |

Note: We rounded up the monthly interest calculation before we added a month's interest to the balance at the beginning of the month. There may be as much as a $\$ 0.03$ difference at the end of the year, as can be seen below in the accumulated balance calculated by using the formula. This \$0.03 difference still yields the same APY.
Michael's $\$ 8,000$ original principal deposit, put into a money market savings account at $2 \%$ APR, compounding monthly, would be worth $\$ \mathbf{8 , 1 6 1 . 4 7}$ at the end of one year.
What APY does this account yield? Again, divide the amount of interest Michael earned for the year by his original principal deposit:
APY $=\frac{161.44}{8000}=0.02018=2.018 \%$
Now, let's try using the formula to calculate Michael's balance at the end of one year:
Principal $(P)=8000$

$$
\operatorname{APR}(r)=2 \%=0.02
$$

$$
n=4 \text { (quarterly) }
$$

$$
t=1 \text { year }
$$

$$
\begin{aligned}
& A=P\left(1+\frac{r}{n}\right)^{n t} \\
& A=8000\left(1+\frac{0.02}{12}\right)^{12 \times 1} \\
& A=8000(1+0.001666)^{12} \\
& A=8000(1.001666)^{12} \\
& A=8000(1.02018) \\
& A=\$ 8.161 .44
\end{aligned}
$$

The formula yields an accumulated balance of $\mathbf{\$ 8 , 1 6 1 . 4 4}$ - or $\$ 0.03$ less than it would be if the calculation were done by hand.

## Now You Try

Ask students to do page 14 of the Now You Try student worksheet.

## Compare Annual vs. Quarterly vs. Monthly Compounding

Discussion Questions

- If the APR is the same on all three investments, which is the best investment? (The investment with the greatest number of compounding periods.)
- How do you think a bank might entice you to open a CD or a statement savings account instead of a money market account? (By offering a higher APR on products that have fewer compounding periods.)


## Assessment

Ask students to complete the assessment worksheet.

## Student Worksheet

## NOW YOU TRY: APR, APY AND COMPOUND INTEREST

## Annual Interest

1. Taylor wants to invest her $\boldsymbol{\$ 7 , 5 0 0}$ college fund at her bank. She picks an annual certificate of deposit that will pay her 3\% interest each year. (Remember, 3\% is 0.03 when written as a decimal.)
A. How much interest will Taylor earn for the year?
B. What will Taylor's balance be at the end of one year?
2. Now, let's say Taylor decides to leave her money in the bank for three years.
A. What is the term of Taylor's certificate of deposit?
B. Fill in the table to find out how Taylor's investment grows.

|  | Beginning Balance | $3 \%$ Interest | Ending Balance |
| :--- | :--- | :--- | :--- |
| Year 1 | $\mathbf{\$ 7 , 5 0 0 . 0 0}$ |  |  |
| Year 2 |  |  |  |
| Year 3 |  |  |  |

Name Date

## Annual vs. Quarterly Interest

3. Taylor wants to invest her $\mathbf{\$ 7 , 5 0 0}$ college fund at her bank. She decides to open a statement savings account, which compounds quarterly, instead of an annual certificate of deposit. This statement savings account will pay her a 3\% APR.
(Remember, $3 \%$ is 0.03 when written as a decimal.)
A. How often does Taylor's account compound?
B. What will Taylor's $1^{\text {st }}$ quarter interest payment be?
C. What will Taylor's balance be when the year is over?

|  | Beginning Balance | $3 \%$ Interest | Ending Balance |
| :---: | :--- | :--- | :--- |
| 1st quarter | $\$ 7,500.00$ |  |  |
| 2nd quarter |  |  |  |
| 3rd quarter |  |  |  |
| 4th quarter |  |  |  |

D. What APY will Taylor's statement savings account earn for the year?

## Compound Interest Formula

There is a formula you can use to calculate the ending balance of an investment if you know certain facts about the investment, such as its principal, APR, compounding periods and the number of years the investment lasts.

> Where: $\boldsymbol{A}=$ Accumulated balance
> $\boldsymbol{P}=$ Principal
> $\boldsymbol{A}=\boldsymbol{P}\left(\mathbf{1}+\frac{\boldsymbol{r}}{\boldsymbol{n}}\right)^{\boldsymbol{n t}} \quad \boldsymbol{r}=$ APR expressed as a decimal
> $\boldsymbol{n}=$ Number of compounding periods per year
> $\boldsymbol{t}=$ Number of years the investment lasts

Let's look again at question 3 on the previous page:
Taylor wants to invest her $\mathbf{\$ 7 , 5 0 0}$ college fund at her bank. She decides to open a statement savings account, which compounds quarterly, instead of an annual certificate of deposit. This statement savings account will pay her a 3\% APR.
(Remember, $3 \%$ is 0.03 when written as a decimal.)
4. What are the...

Principal $=$
APR =
Number of compounding periods =
Number of years the investment lasts = $\mathbf{1}$
... for Taylor's statement savings account?
A. Use the compound interest formula to compute her balance at the end of the year.
B. How does your answer compare to the answer you got when you completed the table in question 3 ?

Name Date

## Quarterly vs. Monthly Interest

Andrea wants to invest $\mathbf{\$ 2 , 0 0 0}$ at her bank. She decides to open a money market savings account, which compounds monthly, instead of a statement savings account. This money market savings account will pay her a 3\% APR.
(Remember, $3 \%$ is 0.03 when written as a decimal.)

$$
A=P\left(1+\frac{r}{n}\right)^{n t}
$$

5. What are the...

Principal =
APR =
Number of compounding periods $=$
Number of years the investment lasts = $\mathbf{1}$
... for Andrea's money market savings account?
A. Use the compound interest formula to compute her balance at the end of the year.
B. What APY will Andrea's money market account earn for the year?

## Student Worksheet: Solutions

## NOW YOU TRY: SOLUTIONS

## Annual Interest

1. Taylor wants to invest her $\$ 7,500$ college fund at her bank. She picks an annual certificate of deposit that will pay her 3\% interest each year. (Remember, $3 \%$ is 0.03 when written as a decimal.)
A. How much interest will Taylor earn for the year? Interest = 7500 x $0.03=\$ 225$
B. What will Taylor's balance be at the end of one year?

Balance $=$ Principal + Interest
Balance $=7500+(7500 \times 0.03)$
Balance $=7500+225=\$ 7,725$
2. Now, let's say Taylor decides to leave her money in the bank for three years.
A. What is the term of Taylor's certificate of deposit?

Three years
B. Fill in the table to find out how Taylor's investment grows:

|  | Beginning Balance | $3 \%$ Interest | Ending Balance |
| :--- | :--- | :--- | :--- |
| Year 1 | $\$ 7,500.00$ | $\$ 225.00$ | $\$ 7,725.00$ |
| Year 2 | $\$ 7,725.00$ | $\$ 231.75$ | $\$ 7,956.75$ |
| Year 3 | $\$ 7,956.75$ | $\$ 238.70$ | $\$ 8,195.45$ |

## Annual vs. Quarterly Interest

3. Taylor wants to invest her $\$ \mathbf{7 , 5 0 0}$ college fund at her bank. She decides to open a statement savings account, which compounds quarterly, instead of an annual certificate of deposit. This statement savings account will pay her a 3\% APR.
(Remember, $3 \%$ is 0.03 when written as a decimal.)
A. How often does Taylor's account compound? Quarterly-four times
B. What will Taylor's 1st quarter interest payment be?

$$
\text { Interest }=\frac{7500 \times 0.03}{4}=\frac{225}{4}=\$ 56.25
$$

C. What will Taylor's balance be when the year is over?

|  | Beginning Balance | $3 \%$ Interest | Ending Balance |
| :--- | :--- | :--- | :--- |
| 1st quarter | $\$ 7,500.00$ | $\$ 56.25$ | $\$ 7,556.25$ |
| 2nd quarter | $\$ 7,556.25$ | $\$ 56.67$ | $\$ 7,612.92$ |
| 3rd quarter | $\$ 7,612.92$ | $\$ 57.10$ | $\$ 7,670.02$ |
| 4th quarter | $\$ 7,670.02$ | $\$ 57.53$ | $\$ 7,727.55$ |

D. What APY will Taylor's statement savings account earn for the year?

$$
\text { APY }=\frac{227.55}{7500}=0.03034=3.034 \%
$$

## Compound Interest Formula

There is a formula you can use to calculate the ending balance of an investment if you know certain facts about the investment, such as its principal, APR, compounding periods and the number of years the investment lasts.

Where: $\boldsymbol{A}=$ Accumulated balance
$A=P\left(1+\frac{r}{n}\right)^{n t}$
$\boldsymbol{P}=$ Principal
$r=$ APR expressed as a decimal
$\boldsymbol{n}=$ Number of compounding periods per year
$\boldsymbol{t}=$ Number of years the investment lasts

Let's look again at question 3 on the previous page:
Taylor wants to invest her $\mathbf{\$ 7 , 5 0 0}$ college fund at her bank. She decides to open a statement savings account, which compounds quarterly, instead of an annual certificate of deposit. This statement savings account will pay her a 3\% APR.
(Remember, $3 \%$ is 0.03 when written as a decimal.)
4. What are the...

Principal $=\mathbf{7 5 0 0}$
APR $=3 \%=0.03$
Number of compounding periods $=4$
Number of years the investment lasts = $\mathbf{1}$
... for Taylor's statement savings account?
A. Use the compound interest formula to compute her balance at the end of the year.

$$
\begin{aligned}
& A=7500\left(1+\frac{0.03}{4}\right)^{4 \times 1} \\
& A=7500(1+0.0075)^{4} \\
& A=7500(1.0075)^{4} \\
& A=7500(1.03034) \\
& A=\$ 7.727 .55
\end{aligned}
$$

B. How does your answer compare to the answer you got when you completed the table in question 3 ?
Both ending balances match, whether done by hand or using the formula.

## Quarterly vs. Monthly Interest

Andrea wants to invest $\mathbf{\$ 2 , 0 0 0}$ at her bank. She decides to open a money market savings account, which compounds monthly, instead of a statement savings account. This money market savings account will pay her a 3\% APR.
(Remember, $3 \%$ is 0.03 when written as a decimal.)

$$
A=P\left(1+\frac{r}{n}\right)^{n t}
$$

5. What are the...

Principal $=\mathbf{2 0 0 0}$
APR $=\mathbf{3 \%}=0.03$
Number of compounding periods $=12$
Number of years the investment lasts = $\mathbf{1}$
... for Andrea's money market savings account?
A. Use the compound interest formula to compute her balance at the end of the year.

$$
\begin{aligned}
& A=2000\left(1+\frac{0.03}{12}\right)^{12 \times 1} \\
& A=2000(1+0.0025)^{12} \\
& A=2000(1.0025)^{12} \\
& A=2000(1.03042) \\
& A=\$ 2.060 .84
\end{aligned}
$$

B. What APY will Andrea's money market account earn for the year?
$A P Y=\frac{60.84}{2000}=0.03042=3.042 \%$

## Student Assessment

## APR, APY AND COMPOUND INTEREST

Taylor has been saving her allowance and her babysitting money for years. She and her friend are planning to travel to Paris, France, when they have each saved enough money.
Taylor has saved $\mathbf{\$ 6 , 5 0 0}$ so far and her friend has saved almost as much. Taylor wants her money to work as hard for her as she has worked to save it!

Taylor's bank has three types of investments to choose from if she wants to put her money to work:

1. Annual certificate of deposit with a $\mathbf{3 . 5 \%}$ APR
2. Statement savings account with a $\mathbf{3 . 2 5 \%}$ APR
3. Money market savings account with a $3.0 \%$ APR

Taylor and her friend have at least one more year before the big trip. Use the compound interest formula to calculate which investment will help Taylor the most.
$A=P\left(1+\frac{r}{n}\right)^{n t}$

Annual CD (compounds annually):

Statement savings account (compounds quarterly):

Money market savings account (compounds monthly):

Name

What are the APYs of each investment?
Annual CD:

Statement savings account:

Money market savings account:

Complete the table, then circle Taylor's best investment choice.

| Investment | APR | APY |
| :--- | :--- | :--- |
| Annual CD | $3.50 \%$ |  |
| Statement savings account | $3.25 \%$ |  |
| Money market savings account | $3.00 \%$ |  |

## Student Assessment: Solutions

Taylor has been saving her allowance and her babysitting money for years. She and her friend are planning to travel to Paris, France, when they have each saved enough money.
Taylor has saved $\$ \mathbf{6 , 5 0 0}$ so far and her friend has saved almost as much. Taylor wants her money to work as hard for her as she has worked to save it!

Taylor's bank has three types of investments to choose from if she wants to put her money to work:

1. Annual certificate of deposit with a $\mathbf{3 . 5 \%}$ APR
2. Statement savings account with a $\mathbf{3 . 2 5 \%}$ APR
3. Money market savings account with a $3.0 \%$ APR

Taylor and her friend have at least one more year before the big trip. Use the compound interest formula to calculate which investment will help Taylor the most.

$$
A=P\left(1+\frac{r}{n}\right)^{n t}
$$

Annual CD (compounds annually):

$$
\begin{array}{ll}
P=6500 & A=6500\left(1+\frac{0.035}{1}\right)^{1 \times 1} \\
r=3.5 \%=0.035 & A=6500(1+0.035)^{1} \\
n=1 & A=6500(1.035)^{4} \\
\boldsymbol{t}=\mathbf{1} & A=\$ 6.727 .50
\end{array}
$$

Statement savings account (compounds quarterly):

$$
\begin{array}{ll}
P=6500 & A=6500\left(1+\frac{0.0325}{4}\right)^{4 \times 1} \\
r=3.25 \%=0.0325 & A=6500(1+0.008125)^{4} \\
n=4 & A=6500(1.008125)^{4} \\
t=1 & A=6500(1.03289) \\
& A=\$ 6.713 .79
\end{array}
$$

Money market savings account (compounds monthly):

$$
\begin{array}{ll}
P=6500 & A=6500\left(1+\frac{0.03}{12}\right)^{12 \times 1} \\
r=3 \%=0.03 & A=6500(1+0.0025)^{12} \\
n=12 & A=6500(1.0025)^{12} \\
t=1 & A=6500(1.03041) \\
& A=\$ 6.697 .67
\end{array}
$$

What are the APYs of each investment?
Annual CD:
$A P Y=\frac{227.50}{6500}=0.035=3.5 \%$

Statement savings account:
$A P Y=\frac{213.79}{6500}=0.03289=3.29 \%$

Money market savings account:
$A P Y=\frac{197.67}{6500}=0.03041=3.04 \%$

Complete the table, then circle Taylor's best investment choice.

| Investment | APR | APY |
| :--- | :--- | :--- |
| Annual CD | $3.5 \%$ | $3.5 \%$ |
| Statement savings account | $3.25 \%$ | $3.29 \%$ |
| Money market savings account | $3.0 \%$ | $3.04 \%$ |

